

Composite Functions

1. If $f(x) = 2x + 1$ and $g(x) = x^2$, find

(a) $f(g(x))$	(b) $g(f(x))$	(c) $f(f(x))$	(d) $g(g(x))$
---------------	---------------	---------------	---------------

2. Given $h(x) = 1 - x$ and $g(x) = \sqrt{x}$, find

(a) $g(16)$	(b) $h(g(16))$	(c) $g(h(x))$	(d) $h(g(x))$
-------------	----------------	---------------	---------------

3. $f(x) = \frac{2}{3x} - 1$ and $g(x) = \frac{2}{3x+3}$.
 - (a) Calculate $f(g(x))$.
 - (b) What is the connection between $f(x)$ and $g(x)$?

4. $f(x) = \sqrt{\frac{x+1}{2}}$ and $g(x) = 2x^2 - 1$.
 - (a) Calculate $f(g(x))$.
 - (b) State the relationship between $f(x)$ and $g(x)$.

5. The function $h(x) = f(g(x))$.
 - (a) Write down $h(x)$ when $f(x) = 2x^2 - 16$ and $g(x) = 2x - 1$.
 - (b) Write $h(x)$ in fully factorised form.
 - (c) For what values of x will the function $\frac{1}{h(x)}$ be undefined?

6. $f(x) = 2x - 1$ and $g(x) = 2x + 1$.
 - (a) Find a formula for $f(g(x))$ and $g(f(x))$.
 - (b) Find the least possible value of $f(g(x)) \times g(f(x))$.

7. $f(x) = \sin x^\circ$ and $g(x) = 3x + 2$
 - (a) Write down an expression for $g(f(x))$.
 - (b) Solve the equation: $g(f(x)) = 1$ $\{0 \leq x \leq 360\}$.